# Compact UHF 3 dB MCCT Power Dividers

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*Abstract*—A compact UHF 3 dB power divider (PD) is presented. It consists of two identical asymmetric impedance transformers (MCCTs) and one isolation circuit with resistance and capacitance. The MCCT is composed of two different transmission-line sections and one open stub, and good frequency performance may be achieved by the combination of transmission-line sections and open stub. One PD is fabricated at a design center frequency of 500 MHz, of which total transmission-line sections are only 39.68° long. The measured bandwidth with 15 dB return loss is about 68%.

*Index Terms*—Asymmetric impedance transformers (MCCTs), compact power dividers (PDs), UHF PDs, Wilkinson power dividers (combiner).

#### I. INTRODUCTION

▶ HE power dividers (PDs) [1]–[11] have been used for various applications such as balanced amplifiers and antenna arrays. As the terrestrial TV applications or wireless communication systems require substantial reduction in mass and volume, compactness of the PDs has been of high interest. There have been several literatures treating compact PDs [3], [5]-[8], [10]. However, the PD in [5] requires two metal layers, which are suitable for MMICs, and two stages are needed for wideband performance. In [6], three dimensional waveguide structures are needed. In [7], two asymmetric equivalent transmission-line sections connected in cascade are employed, but the phase delay doesn't seem to be 90° [8, Fig. 4]. Due to the reason, the isolation circuit should consist of not only resistance but also capacitance (inductance). In [9], lumped-element equivalent circuits (CRLH TLs) are used, but the bandwidths are small. In [10], an etched pattern on ground plane should be involved, probably being suitable only for MMICs. In [3], two-types of modified asymmetric equivalent circuits are exploited, but the application for the PDs with the equal termination impedances is excluded. In [11], the PDs with complex termination impedances are studied, but no compactness is treated for those with real termination impedances.

Manuscript received September 30, 2013; revised December 21, 2013 and January 22, 2014; accepted March 11, 2014. Date of publication June 05, 2014; date of current version June 20, 2014. This work was supported by Basic Science Research Program through the National Research Foundation of Korea (NRF) funded by the Ministry of Education, Science and Technology 2009-0083495.

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Digital Object Identifier 10.1109/LMWC.2014.2316213

15-dB BW Miniaturization Total methods  $(|S_{11}|)$ TL lengths MCCTs with SMTs this work 68% 39.68° and  $L_{S1}$  –type MCCTs, MCVTs 67.72° [3] 80% [7] Asymmetric TLs 133.28°

17.5%

~43%

CRLH TLs

DGS

[9]

[10]

TABLE I

COMPARISONS BETWEEN CONVENTIONAL AND THIS WORKS

In this letter, one type of asymmetric impedance transformers, MCCTs (modified constant conductance-type transmission-line impedance transformers) [3] are investigated in a way different from [3], and a compact PD with 50  $\Omega$  termination impedances is fabricated at a design center frequency of 500 MHz. For the compact PDs, each 90° transmission-line section should be reduced and the frequency performance is determined, depending on how much and in which direction to reduce it. The conventional and this work are compared in Table I where this work may be regarded as the best, considering the compact size.

To verify the best performance, one PD is fabricated and measured at a design center frequency of 0.5 GHz. The total transmission-line sections are 39.68° long, and the 15 dB bandwidth of  $|S_{11}|$  is 68%.

#### II. ASYMMETRIC IMPEDANCE TRANSFORMERS OF MCCTS

The MCCT is depicted in Fig. 1 where two transmission-line sections and one open stub are composed of the MCCT, and the termination impedances are  $2R_L$  and  $R_L$  with the impedance transformation ratio of 2. The characteristic impedances of the transmission-line sections are  $Z_a$  and  $Z_b$  and their electrical lengths are  $\Theta_a$  and  $\Theta_b$ . Those of the open stub are  $Z_o$  and  $\Theta_o$ . Since the MCCT is asymmetric, the termination impedances of  $2Z_L$  and  $Z_L$  cannot be interchangeable. The input impedance looking into the transmission-line section with  $Z_b$  and  $\Theta_b$  is designated as  $Z_{in\_R_L}$ , while that looking into the design formulas for  $Z_a$  and  $\Theta_a$  are obtained as (1a) and (1b), as shown at the bottom of the next page, where

$$Re\left(Z_{in\_2R_L}\right) = \frac{2R_L Z_o^2}{Z_o^2 + \left(2R_L \tan \Theta_o\right)^2}$$
(1c)

$$Im\left(Z_{in\_2R_L}\right) = -\frac{(2R_L)^2 Z_o \tan \Theta_o}{Z_o^2 + (2R_L \tan \Theta_o)^2} \qquad (1d)$$

$$Re\left(Z_{in\_R_L}\right) = \frac{R_L Z_b (1 + \tan^2 \Theta_b)}{Z_b^2 + (R_L \tan \Theta_b)^2}$$
(1e)

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>78.7°

~54.2°



Fig. 1. Asymmetric impedance transformer, MCCT.



Fig. 2. MCCT PD.

$$Im(Z_{in\_2R_L}) = Z_b \frac{(Z_b^2 - R_L^2) \tan \Theta_b}{Z_b^2 + (R_L \tan \Theta_b)^2}$$
(1f)

## III. MCCT PDs

The impedance transformers of MCCTs may be used for the 3 dB PDs. The schematic diagram is depicted in Fig. 2.

For the design of the PDs, the first condition is that the MCCTs are impedance transformers transforming  $2R_L$  into  $R_L$ , and the second condition is that the isolation circuit consisting of  $R_i$  and  $C_i$  should contribute to the perfect isolation between ports (2) and (3). If the isolation impedance produced by  $R_i$  and  $C_i$  is denoted as  $Z_{IC}$ , the following relation should be satisfied:

$$\frac{2}{Z_{IC}} + Y_b \frac{-jY_a \cot\Theta_a + jY_b \tan\Theta_b}{Y_b + (Y_a \cot\Theta_a) \tan\Theta_b} = \frac{1}{R_L}$$
(2)

where  $Y_a = Z_a^{-1}$  and  $Y_b = Z_b^{-1}$ .

Based on the equation in (2), the isolation impedances with  $R_L = 50 \Omega$  were calculated by fixing  $\Theta_b = 10^\circ$  and  $Z_o = 50 \Omega$  and varying  $Z_b$  and  $\Theta_o$ , and the calculation results are plotted in Fig. 3 where a design center frequency is 0.5 GHz and all the values are satisfied with the impedance transforming of MCCTs. When  $Z_b = 200 \Omega$ , the isolation resistances of  $R_i$  are smaller than those with  $Z_b = 160 \Omega$ , and the capacitances of  $C_i$  are also smaller than those with  $Z_b = 160 \Omega$ . Both values of  $R_i$  and  $C_i$  are inversely proportional to  $\Theta_o$  of the open stub in Fig. 2.

## **IV. MEASUREMENTS**

In the fabrication of the MCCT PDs, the first thing is to determine one isolation circuit, because the isolation circuit should be implemented with a set of chip resistor(s) and capacitor(s), and the resistance or capacitance values are limited. In this case,



Fig. 3. Isolation Circuits. (a) Resistance. (b) Capacitance.



Fig. 4. SMT with N = 3 (Stepped-impedance modified T-type).

 $Z_b = 200 \ \Omega, \Theta_b = 10^\circ$  and  $\Theta_a = 7.2^\circ$  are chosen to have the isolation impedance of  $(64.725 - j47.78) \ \Omega$  in Fig. 3. The isolation circuit may be implemented with two chip resistors of 62 and 2.7  $\Omega$  and two capacitors of 5.6 and 1.2 pF at 0.5 GHz. In this case,  $Z_a = 55.79 \ \Omega$  and  $\Theta_a = 28.77^\circ$  are, based on (1), calculated. The transmission-line section with  $Z_a$  and  $\Theta_a$  in Fig. 2 may be reduced more by use of a symmetric equivalent circuit of SMT [12, Fig. 6(b)], and the relation is described in Fig. 4 where only three stages (N = 3) are shown.

Letting  $\Theta_{pa} = 0^{\circ}$  in Fig. 4(b) [13, Fig. 6(b)], the characteristic impedance of  $Z_{sT}$  and the total electrical length of  $3\Theta_{sT}$ are computed as  $Z_{sT} = 114.858 \Omega$  and  $3\Theta_{sT} = 14^{\circ}$ .

The transmission-line section with  $Z_b = 200 \ \Omega$  and  $\Theta_b = 10^{\circ}$  in Fig. 2 may also be reduced by an equivalent circuit of  $L_{S1}$ -type [14, Fig. 6(d)] where the  $L_{S1}$ -type consists of  $N_s$  number of  $L_{S1}$  inductance and two identical transmission-line

$$Z_{a} = \sqrt{\frac{Re(Z_{in\_R_{L}}) |Z_{in\_2R_{L}}|^{2} - Re(Z_{in\_2R_{L}}) |Z_{in\_R_{L}}|^{2}}{Re(Z_{in\_2R_{L}}) - Re(Z_{in\_R_{L}})}}$$
(1a)

$$\tan \Theta_a = Z_a \frac{Re\left(Z_{in\_R_L}\right) - Re\left(Z_{in\_2R_L}\right)}{Re\left(Z_{in\_2R_L}\right) Im\left(Z_{in\_2R_L}\right) - Re\left(Z_{in\_2R_L}\right) Im\left(Z_{in\_R_L}\right)}$$
(1b)



Fig. 5. Fabricated MCCT PD.



Fig. 6. The results measured and predicted are compared. (a) Power division and matching at port 1; (b) Isolation and matching at port 2.

sections with the characteristic impedance of  $Z_{LS1}$  and electrical length of  $\Theta_{LS1}/2$ . For that with  $Z_b = 200 \ \Omega$  and  $\Theta_b = 10^\circ$ ,  $N_s = 1$  was chosen, which results in  $Z_{LS1} = 116.56 \ \Omega$ ,  $\Theta_{LS1} = 5.84^\circ$  and  $L_{S1} = 7.3 \ \text{nH}$  at 0.5 GHz. The fabricated MCCT PD is shown in Fig. 5 where the total transmission-line sections are 39.68° long. That is, a 90° transmission-line sections is reduced to a 19.84° one.

The frequency responses measured and predicted are compared in Fig. 6 where the power division and the matching at port ① are in Fig. 6(a), and the isolation and the matching at port ② in Fig. 6(b). The measured results are in good agreement with the predicted ones, and the bandwidth with 15 dB return loss at port ① is 68% (0.32–0.66 GHz). That at port ② is 96% (0.31–0.79 GHz) and the 15 dB isolation is 94% (0.25–0.72 GHz). Since the bandwidth is determined by the worst performance, the bandwidth of the MCCT PD in Fig. 5 is 68%, which may be considered as a good result for the compact size.

### V. CONCLUSION

In this letter, a compact UHF MCCT PD is presented. The MCCT consists of two different transmission-line sections and one open stub, and the frequency performance better than that of any other symmetric one is generated by the combination of three elements in MCCTs. Therefore, even though the total transmission-line sections of the MCCT PD are only 39.68 ° long, quite being compact, the measured bandwidth is 68%. As the results of their desirable property for the compact size, the MCCT PDs can be used in a UHF frequency region.

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